

Modelling the Value of an Airport Slot

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Slots at Congested Airports



- Many airports are at full capacity for aircraft movements
- New runway infrastructure often prohibited
 - Local and/or global environmental impacts
 - Planning and space restrictions
 - Cost
- One current solution is slot allocation
- A method for finding slot value is sought by airlines, airports and governments
- **Objective is to determine slot value, focusing on Gatwick Airport**

Modelling the Value of an Airport Slot: Important components to consider

DESTINATION	FLIGHT	GATE
LONDON	BA 903	31
SYDNEY	QF5723	27
TORONTO	AC5984	22
TOKYO	JL 608	41
HONG KONG	CX5471	29
MADRID	IB3941	30
BERLIN	LH5021	28
NEW YORK	AA 997	11
PARIS	AF5870	23
ROME	AZ5324	43

easyJet	07:25	2h 40	→	11:05	10 deals from £42
	LGW	Direct		MAD	
easyJet	16:45	2h 25	→	18:10	Select →
	MAD	Direct		LGW	

- Current operations of the airline

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- Current operations of the airline
- Competitor airlines' operations
- Passenger behaviour
- A profit motive for the airlines
- **The Airline Behaviour Model (ABM) encapsulates this**



ABM: Airline Behaviour Model

- Objective function: each airline (M) sequentially maximizes profits (P) within its network
- Decision variables: airfare (Fare), flight frequency (Freq) of type of aircraft (a)

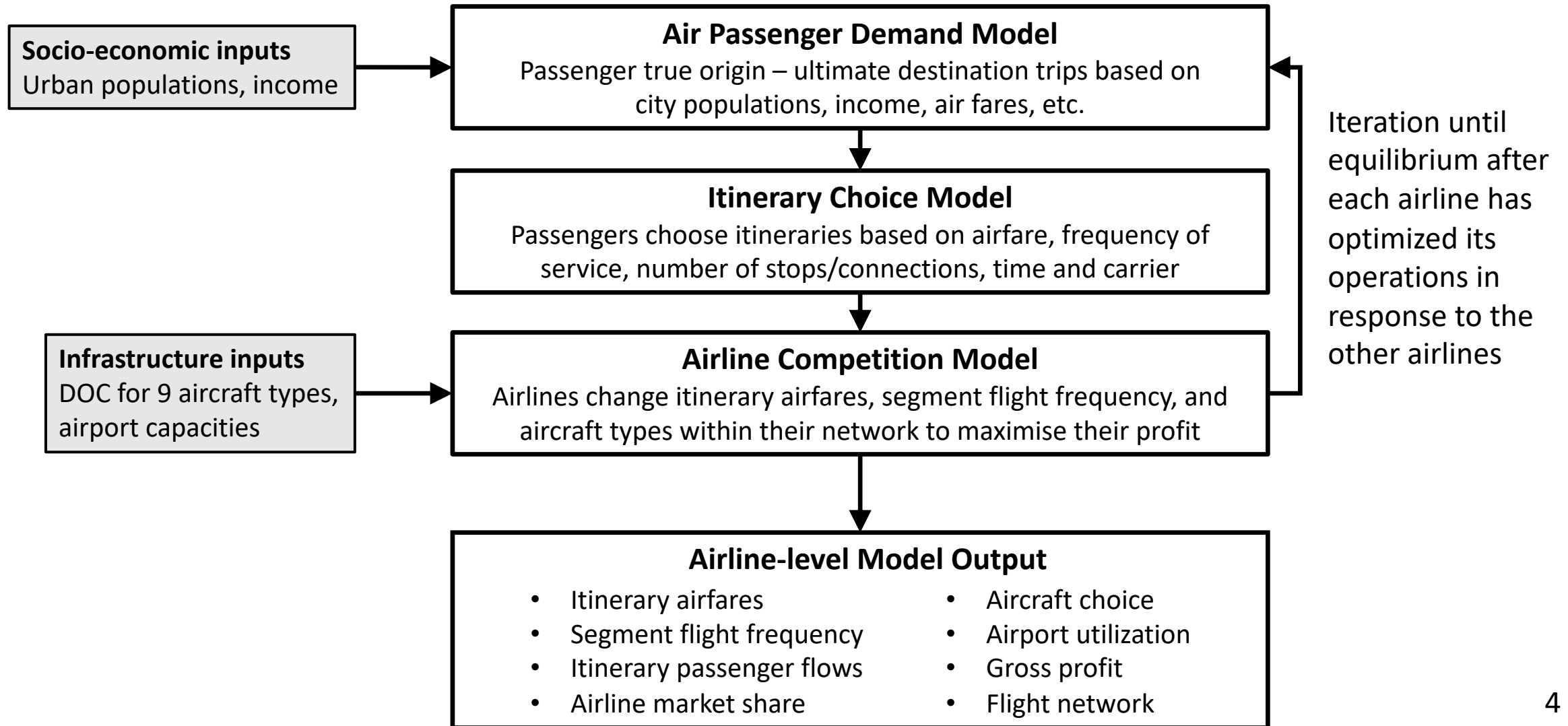
$$P_M = \underbrace{\sum_{i \in ITN_M} (Fare_i \cdot Pax_i + Arev_M \cdot Pax_M)}_{\text{Revenues}} - \underbrace{\sum_{j \in SEG_M} \sum_{a \in AC_j} Op_{cost_{a,j}} \cdot Freq_{a,j}}_{\text{Flight-related costs}} - \underbrace{\sum_{j \in SEG_M} \sum_{a \in AC_j} Pax_{cost_{a,j}} \cdot Pax_{a,j}}_{\text{PAX-related costs}}$$

- Set of linearized constraints
 - E.g. Airport capacity constraint:

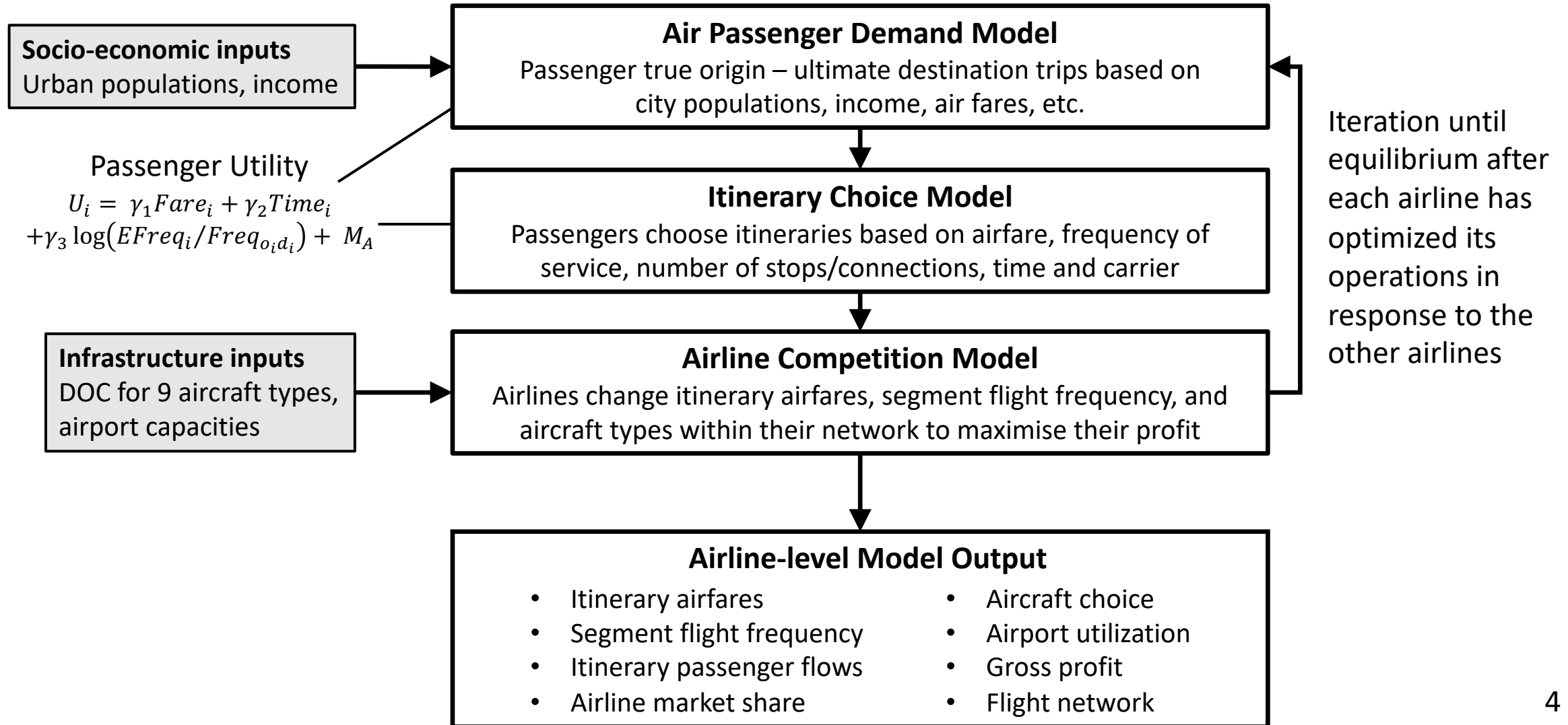
$$\sum_{j \in SEG_p} \sum_{a \in CRFT_j} Freq_{a,j} \leq max_p \quad \forall p \in APT,$$

- Airlines take turns incrementally adjusting decision variables
- Iterate until profit equilibrium

ABM: Airline Behaviour Model



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ABM: Adapted for Slot Prices

- Add an extra term to the Airline objective (profit) function:

$$P_M = \sum_{i \in ITN_M} Fare_i \cdot Pax_i + Arev_M \cdot Pax_M - \sum_{j \in SEG_M} \sum_{a \in AC_j} Opccost_{a,j} \cdot Freq_{a,j} - \sum_{j \in SEG_M} \sum_{a \in AC_j} Paxcost_{a,j} \cdot Pax_{a,j} - C_p \cdot N_{M,p}$$

- Adjust the model constraints:

When making additional
(purchasable) slots available:

$$\sum_{j \in SEG_p} \sum_{a \in CRFT_j} Freq_{a,j} \leq max_p + N_{M,p}$$

$$N_{M,p} < 2 \times 365$$

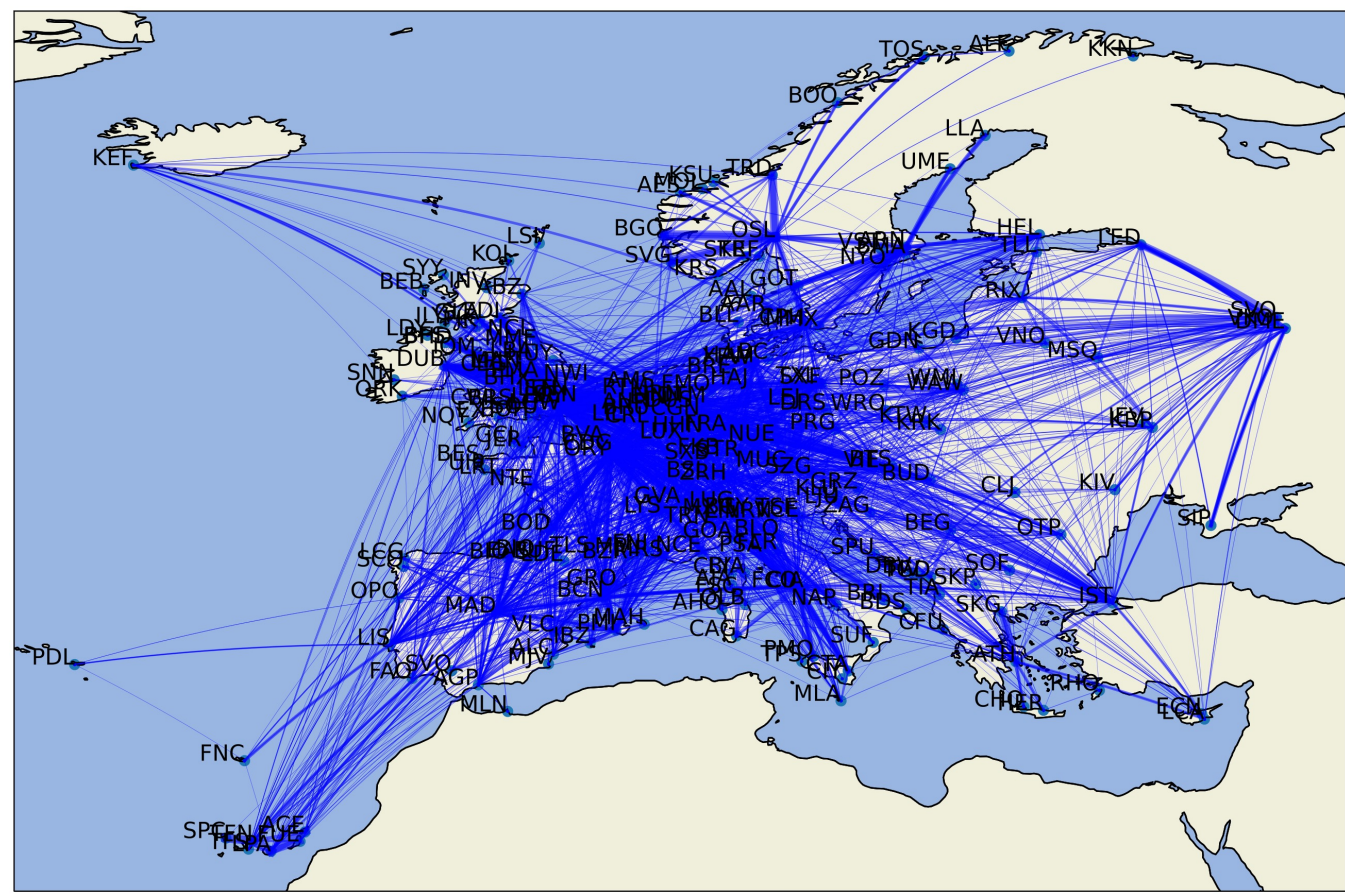
When emulating the sale of
all slots at an airport:

$$\sum_{j \in SEG_{M,p}} \sum_{a \in CRFT_j} Freq_{a,j} \leq N_{M,p}$$

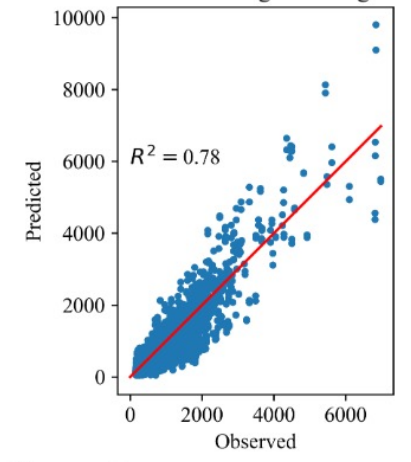
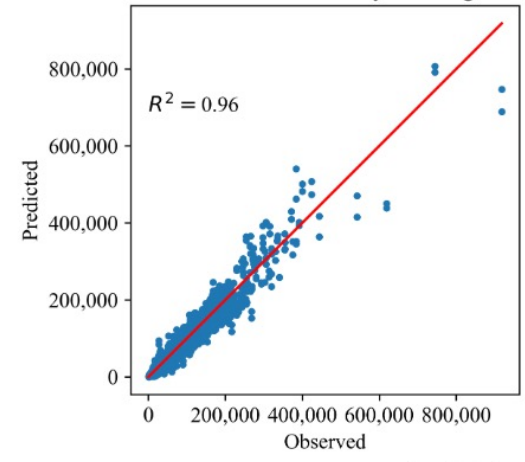
$$\sum_M N_{M,p} \leq max_p$$

- Vary the cost, C_p , and see if airlines acquire the slots

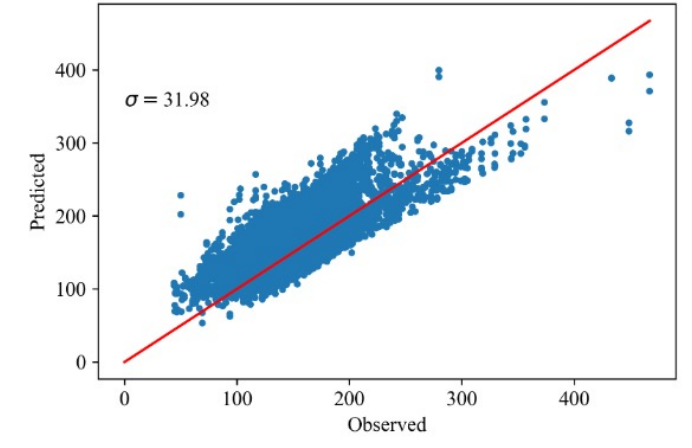
Airline Behaviour Model (ABM): Trained and calibrated over Europe



Predicted versus Actual Itinerary Passenger Numbers Predicted versus Actual Segment Flight Frequencies



Predicted versus Actual Segment Fares



Airline Behaviour Model (ABM): Results for Gatwick Airport



- Two dominant airlines:



Airline Behaviour Model (ABM): Results for Gatwick Airport



- Two dominant airlines:



- **Sale of extra slots at Gatwick**

(use amortization formula)

Price of a single slot ->	annual price of a daily slot-pair.	->	indefinite rights
\$150-175	\$110,000-128,000		\$2.2-2.6 million

- Easyjet highest bidder (followed closely by British Airways)

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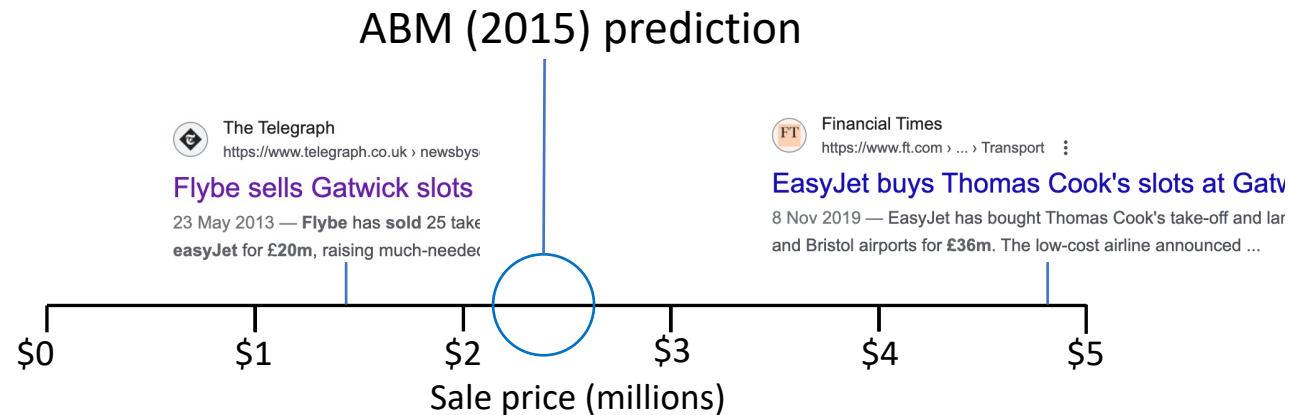


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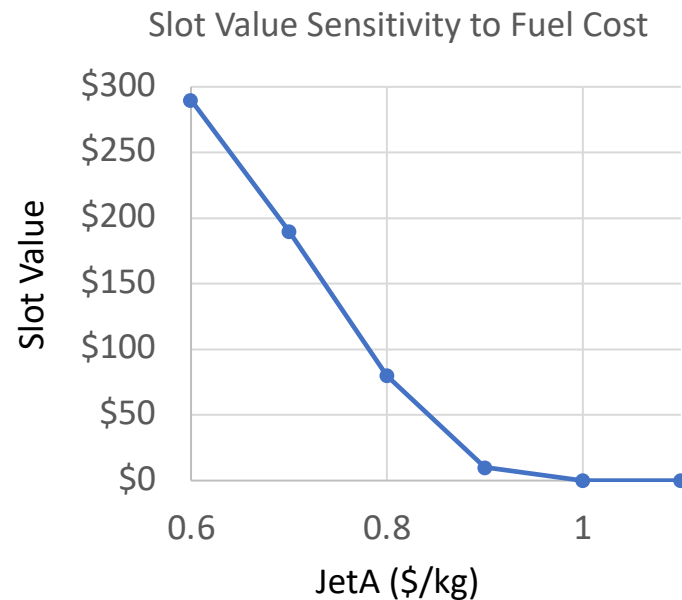


Airline Behaviour Model (ABM): Results for Gatwick Airport

- **Sale of all slots at Gatwick airport**
 - Up to \$190 per slot, all remain utilised.
 - Above \$190, Gatwick dips below full capacity
- Suggests average daily slot-pair price of \$137,000 p.a.

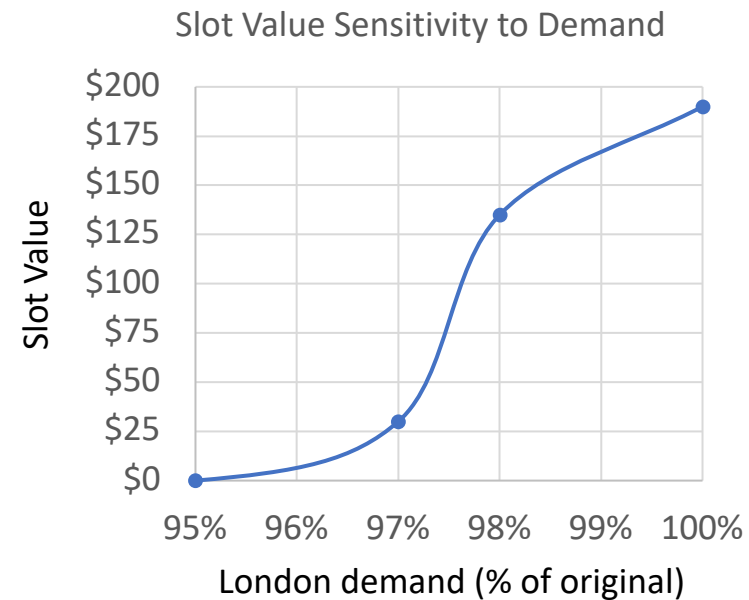
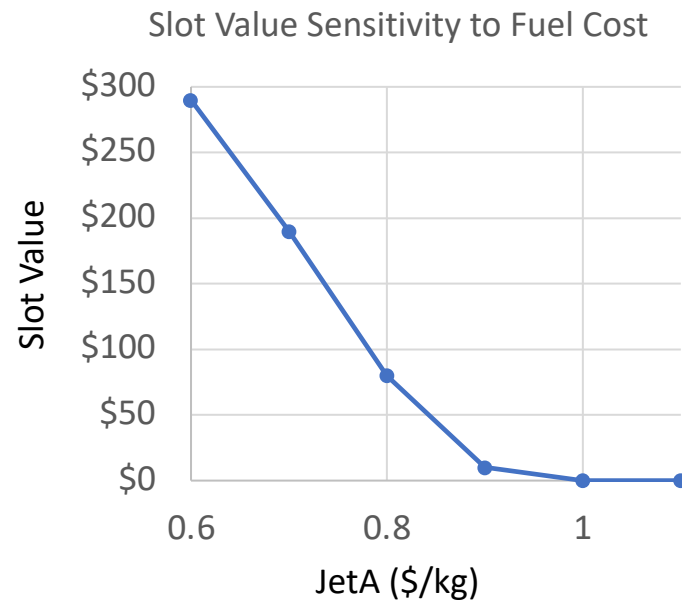
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Airline Behaviour Model (ABM): Conclusions and Further Work

- Have used ABM to predict slot value at Gatwick airport
- Method is generalisable. Can be used for any/many airports
- Allows for a range of scenarios to be examined
- Can quantify the effects of exogenous changes (fuel price, demand)

- Caveats:
 - Lack of external buyers/new entrants
 - Yearly average slot value only
 - Model only covers Europe

- Further Work:
 - Expand ABM to global coverage

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